

# **A Deep Belief Network for the Acoustic-Articulatory Inversion Mapping Problem**

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## **Abstract**

In this work, we implement a deep belief network for the acoustic-articulatory inversion mapping problem.

We find that adding up to 3 hidden-layers improves inversion accuracy. We also show this is due to the higher expressive capability of a deep model and not a consequence of adding more adjustable parameters. Besides, we show unsupervised pretraining of the system improves its performance in all cases, even for a 1 hidden-layer model.

Our implementation obtained an average root mean square error of 0.95 mm on the MNGU0 test dataset, beating all previously published results.

## **Acknowledgements**

Thanks to Steve Renals and Korin Richmond, for their encouragement, patience and teachings. It has been a pleasure working with such knowledgeable and approachable supervisors.

Thanks as well to Iain Murray, and all the people at the ANC, for giving me unlimited access to their GPU equipment. Without them I would still be waiting.

## **Declaration**

I declare that this thesis was composed by myself, that the work contained herein is my own except where explicitly stated otherwise in the text, and that this work has not been submitted for any other degree or professional qualification except as specified.

*(Benigno Uría)*



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# Chapter 1

## Introduction

Speech sounds are produced by the passage of air, pushed out by the lungs, through the larynx and the vocal tract<sup>1</sup>. The quality of the sound formed depends on the position of the vocal folds and the shape of the vocal tract [24]. The different parts of the vocal tract that modify its shape are called the vocal tract articulators. The vocal tract articulators include: the lips, the jaw, the velum<sup>2</sup>, and the tongue. These are shown in Figure 1.1.

The acoustic-articulatory inversion mapping problem (or simply articulatory inversion) is that of trying to infer the position of the vocal tract articulators from an acoustic speech signal. It can be posed as a regression problem in which the speech signal is the observed variable and the position of the articulators is the variable to infer.

The non-linear nature of articulatory inversion, along with the fact that several articulator positions can generate the same sound, make articulatory inversion a challenging problem.

A system capable of approximating the position of the articulators from the acoustic signal would find several applications:

- Speech recognition. Articulatory information can improve the performance of automatic speech recognition systems [53, 28].
- Speech synthesis. Articulatory information can be used to improve the quality or to modify the characteristics of the synthesized voice [26].
- Character animation. Inversion mapping can automate the facial animation of virtual characters in films and video-games [20].
- Speech training. Being able to infer and visualize the position of the articulators would be useful in speech therapy systems for the hearing impaired.

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<sup>1</sup>The vocal tract consists of all air passages above the larynx.

<sup>2</sup>The velum is a soft part of the palate that can be moved to touch the back of the pharynx closing the nasal tract.

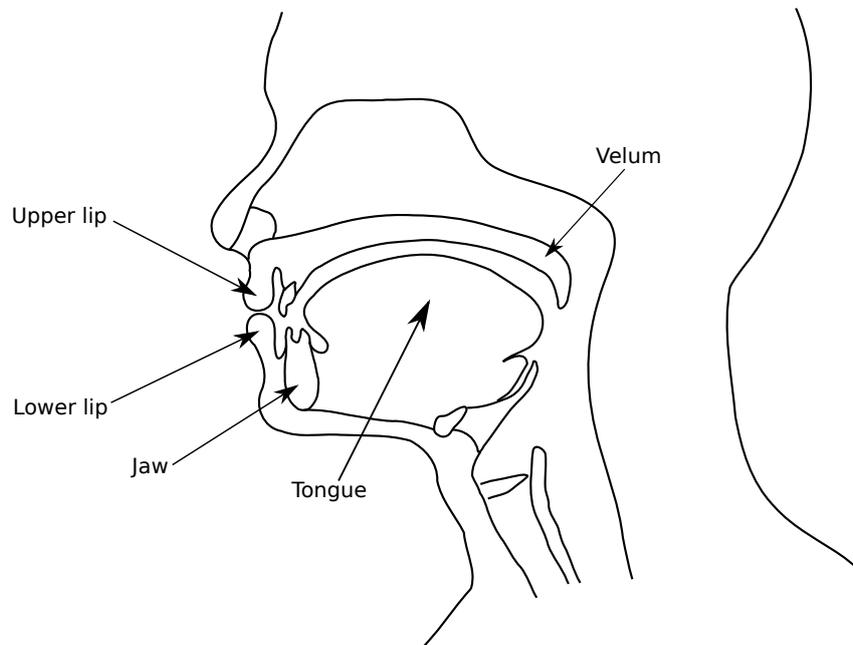


Figure 1.1: Vocal tract articulators shown on a midsagittal section of the head.

- Very low bit-rate speech coding. Speech can be synthesized back from the position of the vocal tract articulators, and very low sampling rates are needed.

Several mathematical techniques have been applied in the past to tackle the articulatory inversion problem. The introduction of rich articulatory datasets of precise quantitative articulatory position data along with recordings of the acoustic data produced, has made it possible to use standard machine learning methodologies like artificial neural networks [44] or hidden Markov models [19, 56].

Artificial neural networks with more than one or two hidden layers have usually been considered too difficult to train to be of practical use [3]. However, they have become a practical option after new theoretical insights on the potential advantages of this kind of deep architectures [3], and the introduction in 2006 of an algorithm capable of training an artificial neural network with many hidden layers, by first training a deep generative model called deep belief network [18].

Deep architectures (more specifically, deep belief networks) have recently been used to obtain state-of-the-art accuracies in phone classification [30, 10, 33, 32, 31, 22] (i.e. in classifying speech acoustic signals into phonemes). Motivated by these successes in phone recognition, and given its similarities with articulatory inversion, we hypothesised a deep belief network would be able to obtain high accuracy in articulatory inversion.

In this work we have implemented a deep belief network for articulatory inversion. We have evaluated its performance using the MNGU0 test dataset for which we obtained a root mean squared error (RMSE) of 0.95 mm. A significant improvement with respect

to the best previously published results of 0.99 mm obtained by Richmond [46] using a trajectory mixture density network. This favourable result leads us to conclude that deep architectures are a suitable approach to articulatory inversion. Furthermore, given that our implementation uses a very simple dynamical model, we hypothesise an even higher degree of accuracy could be obtained using a more elaborate trajectory model which we propose as future work.

The rest of this dissertation is organized as follows: in Chapter 2, we will review the previous literature on articulatory inversion. After that we will introduce the functioning of deep architectures, focusing on deep belief networks. Then, we will review the previous literature on the use of deep belief networks in speech processing more specifically, in phone classification. In Chapter 3, we will introduce the dataset and evaluation criteria we will use to judge the performance of our system. In Chapter 4, we will detail our implementation, analyse its performance and discuss the different implementation variants we have tried, comparing them with each other and with results from previous research. To finish, in Chapter 5 we will draw some conclusions and outline future research directions we intend to pursue.



## Chapter 2

# Background

### 2.1 Previous approaches to articulatory inversion

#### 2.1.1 Early approaches: synthetic datasets

Early work on the acoustic-articulatory inversion problem was hampered by the lack, at the time, of precise quantitative data on articulator-position acoustic-signal correspondences. Two different approaches were taken to avoid this obstacle:

1. Inversion by mathematical analysis of the speech signal in order to calculate the size of the resonance tubes that could have produced it. These techniques have several disadvantages: they are only suitable for a small subset of sounds like vowels and some voiced consonants, it is not easy to find out whether the areas calculated are physically possible to articulate, and they require special measurement techniques of the acoustic signal [44].
2. Use of computer simulations of the vocal tract in order to produce synthetic datasets of articulator-position to acoustic-output correspondences [1, 40, 12], which are then used to train standard regression techniques.

The work of Atal et al. [1] in 1978 is an example of inversion using synthetic datasets. In their work, the authors generated a codebook of many articulator-position acoustic-output pairs by simulating a vocal tract while regularly varying four articulator position parameters. Once the codebook had been created, inversion was done simply by looking up in the codebook the articulator configuration corresponding to the best match for the acoustic input to invert. In their work, Atal et al. noticed that some sounds can be produced by several articulator configurations. The solution, therefore, may be non-unique, making articulatory inversion an ill-posed problem.

Fifteen years later, in 1993, Rahim et al. [40] proposed the use of an assembly of artificial neural networks trained on a synthetically generated dataset and fine-tuned with real speech data. Each ANN is in charge of one of 128 regions of the articulatory space. Each neural network is responsible for detecting speech signals articulated in its designated region. To perform inversion, the 6 regions of articulatory space corresponding to the 6 better matching neural networks were selected. Dynamic programming was then used to infer the path of the articulators through the series of selected networks. In this way, Rahim et al. report that their system is capable of dealing with the non-uniqueness problem. Inversion performance improves compared to the work of Atal et al. Moreover, using an assembly of neural networks required less memory than storing a complete codebook and estimation was faster than a codebook lookup. Furthermore, a big codebook of synthetic data could be used during training without affecting the performance during inference.

Shirai and Honda [12] proposed the use of Kalman filters [23] for articulatory inversion. In a regular Kalman filter there is a linear function that transforms state variable values into visible variable values. In this case, the state variables represent the position of the articulators while the observable variables hold the acoustic data. They were very successful inferring the position of the articulators for vowels and vowel sequences. However, the system gave poor results for other kinds of sounds.

### 2.1.2 Articulography and EMA datasets

Several different methods have been developed in order to measure the position of the vocal tract articulators during speech production. X-ray cinematography provides accurate imaging of the articulators. However, sustained exposure to X-ray radiation is, unfortunately, dangerous; making it impractical for the creation of extensive parallel acoustic and articulator-position datasets. X-ray microbeam cinematography and MRI recording reduces the health-risk factor, but is technically difficult and requires expensive equipment [44]. Electromagnetic midsagittal articulography (EMA), a technique that uses electromagnetic transducer coils glued to the vocal-tract articulators to record precise measurements of their position [36], has become the most widely used articulography technique for the creation of parallel acoustic and articulator-position recordings due to its relative simplicity of use and low cost.

The principles underlying EMA are simple: several fixed coils are fed with alternating currents, generating an electromagnetic field which in turn induces a current on a set of receiver coils placed on the articulators (see Figure 2.1). The voltage induced is approximately inversely proportional to the cube of the distance from the transmitter coils. By measuring the current passing through each transducer coil, it is possible to calculate the distance from each transmitter coil and triangulate its position. Taking measurements at regular intervals

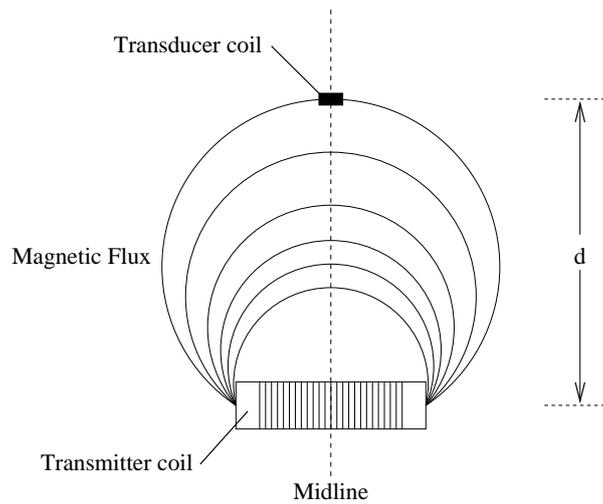


Figure 2.1: Diagram showing EMA working principles. A fixed transmitter coil (bottom) generates an alternating magnetic field which induces a current on the transducer coil (top). Image courtesy of Korin Richmond.



Figure 2.2: Photograph of an EMA recording session. Positioning of the articulator tracking coils is clearly visible. Image courtesy of Korin Richmond.

allows EMA equipment to record the trajectory of each articulator.

Figure 2.2 shows a photograph from an EMA recording session displaying the articulograph equipment and coil placement.

The introduction, during the 1990's, of parallel EMA and acoustic recording datasets, allowed the research community to switch their focus away from the creation of accurate synthetic datasets, to the use of more advanced machine learning techniques.

### 2.1.3 Modern approaches: Learning from EMA data

In 1998 Dusan and Deng [12] proposed using extended Kalman filters for the articulatory inversion problem. Extended Kalman filters are similar to regular Kalman filters but the function that transforms state variable to observed variables has no linearity constraint. They reported a root mean square error (RMSE) of 2 mm on their own EMA dataset.

In 2002 Hiroya and Honda [19] took a different approach suggesting the use of hidden Markov models [39]. Their system is made up of HMMs of articulatory parameters for each phoneme and an articulatory-to-acoustic function for each state. They use maximum a posteriori estimation of the articulatory states for the acoustic input presented. Unfortunately, their system has to be fed with phonemic information input to obtain good results. Hiroya and Honda reported a 1.50 mm RMSE with phonemic information and 1.73 mm RMSE without it, on their own EMA dataset.

In his doctoral thesis, also in 2002, Richmond [44] created an inversion system based on artificial neural networks (ANN) trained using acoustic and EMA data from the MOCHA-TIMIT dataset [55]. Richmond raised a concern about his artificial neural network system, the problem of non-uniqueness: several configurations of the vocal articulators can produce the same sound.

To tackle the non-uniqueness problem in an explicit manner, Richmond also implemented a mixture density network (MDN) [44], a methodology first proposed by Bishop [5]. A MDN uses a ANN to calculate the parameters of the components of a mixture model (usually Gaussian), mapping the input to a (potentially multi-modal) probability distribution (instead of a point) in the output space. The experimental setup is similar to the one used for ANN. However, in this case 14 separate MDNs were trained (one for each dimension of movement of seven articulators) using 2 Gaussians for the output density mixtures, each Gaussian requiring a mixing factor, a mean and a variance. Although, Richmond's initial work obtained what, at the time, were state-of-the-art results of 1.42 mm average RMS error on the MOCHA-TIMIT dataset, it did not use any dynamic constraints, just a low pass-filter of the output to account for the slowly varying nature of articulator movement compared to acoustic data.

In order to take into account the dynamic constraints of articulatory movements, a statistical trajectory model can be used. These kind of models augment the output with dynamic (delta and delta-delta) features and then use these position, velocity and acceleration estimation series to calculate the most likely trajectory.

An example of a trajectory model is that proposed in 2008 by Zhang and Renals' [56]: a trajectory hidden Markov model using a two-stream HMM where acoustic recognition and articulatory synthesis are modelled jointly. To perform inversion mapping with this

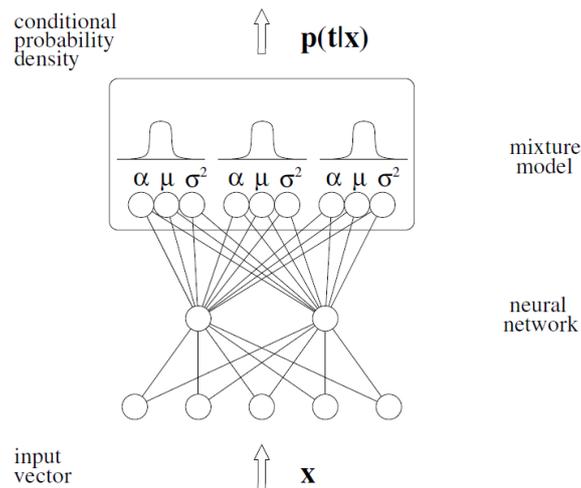


Figure 2.3: Diagram of a mixture density network. Image courtesy of Korin Richmond.

system, first the state alignment for the appropriate HMM is derived from the acoustic observation data. Then, the articulatory observation data is synthesised. In order to account for the dynamic nature of the articulator’s positions the output is augmented with delta and delta-delta features for each coordinate of each articulator. This delta-augmented estimation is finally processed by a maximum likelihood parameter generator [54] that produces the maximum likelihood trajectory of each articulator. Unfortunately, like Hiroya and Honda’s HMM system, it requires the input of phonemic information added to the acoustic data to obtain good results. Using only the acoustic speech signal the system obtained an RMS error of 1.705 mm on the MOCHA-TIMIT dataset.

Trajectory mixture density networks [45] (TMDNs) are an extension of Richmond’s previous work implementing a trajectory model. A TMDN is made up of MDNs trained to output not only static (position), but also dynamic features (velocity and acceleration). Then a maximum likelihood parameter generator algorithm (MLPG) is used to obtain the maximum likelihood trajectory. This method was found to obtain better results than a static MDN even if its output was low-pass filtered. It achieves an RMS error of 1.37 mm on the MOCHA-TIMIT dataset and just 0.99 mm on the much more precise MNGU0 dataset<sup>1</sup>.

In 2010 Ling et al. [27] published an analysis of HMM-based articulatory inversion using trajectory methods. They measured the accuracy of the system on the MNGU0 dataset, obtaining an average RMS error of 1.076 mm when using only acoustic information as input.

Unfortunately, several different EMA datasets were used to report the accuracy of the different methodologies, which makes it difficult to compare their performances. However, MOCHA-TIMIT has been the most widely used EMA dataset, on which Richmond’s tra-

<sup>1</sup>The differences between these two datasets will be further explained in Chapter 3

jectory mixture density networks are considered the state-of-the-art.

## 2.2 Deep architectures

### 2.2.1 Introduction

From the early beginnings of artificial intelligence as a scientific discipline, pattern recognition methods structured in several layers, each representing the input at increasing complexity levels of abstraction, have been frequently proposed [34].

The first description of a multi-level model of pattern recognition is, probably, the pandemonium architecture, proposed by Selfridge in 1959 [51]. Pandemonium is structured in several feed-forward layers of “daemons” (computing elements) that send messages to the daemons on the layer directly above it.

Another early example is the blackboard model [14], introduced in the 1970’s, which depicts a system of computer programs (“knowledge systems” in the blackboard terminology) that interact with each other by reading and writing the blackboard (a set of attributes structured in levels of abstraction). Any knowledge system is allowed to read or write any level of the blackboard, but will typically only interact with a subset.

Even though, the Pandemonium model was used in the design of character recognition systems [34], and the Blackboard model was used in speech recognition [13], they both are just architectures, not actual pattern recognition algorithms. The processing done by the daemons or the knowledge systems, still had to be hand-crafted for each recognition task, requiring expert knowledge about the problem domain.

Multi-layer neural networks had been described, and studied, during the 1950’s and 1960’s [34]. However, until the 1980’s, the only kind of neural networks for which a supervised training algorithm was known was the perceptron [48]. A perceptron, is made up of an input and an output layer and is in effect a linear discriminant, which severely limits its ability to represent complex transformations. In 1986 Rumelhart et al. [49] introduced a supervised method, called backpropagation, capable of training neural networks with hidden layers. This multi-layered neural networks, which overcome the expressive limitations of perceptrons, have been widely successful in their application [11].

Alas, in practice, it is generally admitted that backpropagation is only useful when using one or at most two hidden layers, and will offer poor results as more layers are added. The explanation for this [17, 4] is that if the initial connection weights are chosen to be small, it is very difficult to train the network because the gradients will decrease multiplicatively. However, if the initial values are high (randomly choosing a region of the weight space),

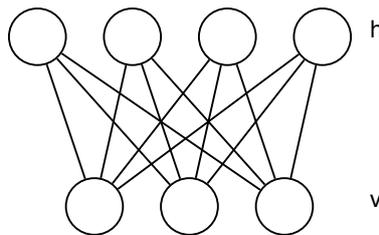


Figure 2.4: Graphical model of a restricted Boltzmann machine with 3 visible units and 4 hidden units.

it is very probable that the learning process will get trapped in a local optimum near that region.

In the last decade, learning deep models has been made possible using an unsupervised learning algorithm that learns generative models called deep belief networks (DBN) one layer at a time [18].

Both, single-hidden-layer networks and deep belief networks are universal approximators [21, 25], i.e. both can approximate any function to an arbitrary degree of accuracy. However, the issue is not if it is possible to model a solution using a given architecture, but if it is feasible to learn a solution given the limited amount of computing resources and training data. Bengio and LeCun proved [2] that, for example, in order to implement the parity function of a  $d$ -dimensional input, a support vector machine [9] with a Gaussian kernel will require  $O(2^d)$  support vectors, and a single-hidden-layer neural network will have to learn  $O(d^2)$  connection weights. In contrast, a deep architecture with  $d$ -hidden layers can represent the parity function using just  $O(d)$  parameters.

### 2.2.2 Restricted Boltzmann machines

Restricted Boltzmann machines (RBMs) [16] are not deep architectures. They are undirected graphical models formed by two layers of probabilistic binary units: a visible layer  $\mathbf{v}$ , and a hidden layer  $\mathbf{h}$ . All units are fully connected to the units in the other layer and no connections between units of the same layer are present (see Figure 2.4). RBMs are relevant to deep models in that they are the building block out of which deep belief networks are constructed one layer at a time (see section 2.2.3 on page 14).

Restricted Boltzmann machines are energy-based models. They capture dependencies between variables by assigning an energy value to each configuration, with more probable configurations having a lower energy. The energy for a given configuration is given by the expression:

$$E(\mathbf{v}, \mathbf{h}) = -\mathbf{v}^T W \mathbf{h} - \mathbf{b}^T \mathbf{v} - \mathbf{c}^T \mathbf{h}$$

where  $W$  is the matrix of connection weights,  $\mathbf{b}$  is the vector of visible layer biases and  $\mathbf{c}$  is

the vector of hidden layer biases.

The probability of a given configuration will be:

$$P(\mathbf{v}, \mathbf{h}) = \frac{1}{Z} e^{-E(\mathbf{v}, \mathbf{h})}$$

where  $Z = \sum_{\mathbf{v}, \mathbf{h}} e^{-E(\mathbf{v}, \mathbf{h})}$

Because no connections exist between units of the same layer, the probability of the units in the top two layers factorize given the state of the other layer (i.e. the state of the units in one layer are conditionally independent given the state of the units in the other layer), and have the expression:

$$P(\mathbf{v}_j = 1 \mid \mathbf{h}) = \sigma(-\mathbf{b}_j - W_{j \cdot} \mathbf{h}) \quad (2.1)$$

$$P(\mathbf{h}_j = 1 \mid \mathbf{v}) = \sigma(-\mathbf{c}_j - W_{\cdot j}^T \mathbf{v}) \quad (2.2)$$

where,  $\sigma$  is the logistic sigmoid function  $\sigma(x) = \frac{1}{1+e^{-x}}$ ,  $W_{\cdot j}$  corresponds to the  $j$ -th column of the weights matrix, and  $W_{j \cdot}$  to the  $j$ -th row.

Sampling from the distribution modelled by the RBM can be done by performing Gibbs sampling [8], initialising all units to arbitrary values and updating the two layers alternately using equations 2.1 and 2.2.

RBM's can be used as associative memories. To sample from this memory, the state of some of the units is clamped and Gibbs sampling is performed to obtain the state for the rest of units.

Training an energy based model to capture a probability distribution is done by reducing the energy of the more probable regions of the state space, and increasing the energy of the less probable ones. “Shovelling” energy from regions of higher probability to regions of lower probability [4].

Maximum likelihood learning in an RBM can be done using the following expressions [16]:

$$\Delta W_{ij} = \langle \mathbf{v}_i \mathbf{h}_j \rangle_0 - \langle \mathbf{v}_i \mathbf{h}_j \rangle_\infty$$

$$\Delta \mathbf{b}_i = \langle \mathbf{v}_i \rangle_0 - \langle \mathbf{v}_i \rangle_\infty$$

$$\Delta \mathbf{c}_i = \langle \mathbf{h}_i^1 \rangle_0 - \langle \mathbf{h}_i^1 \rangle_\infty$$

where:

- $\langle \cdot \rangle_0$  denotes the average when the visible units are clamped to the input values and the hidden units are sampled from their conditional distribution (Equation 2.2).
- $\langle \cdot \rangle_\infty$  denotes the average after assigning the input data to the visible units and running Gibbs sampling until the stationary distribution is reached.

Unfortunately, maximum likelihood learning is too slow to be applied in a practical setting. An alternative often used is contrastive divergence (CD) learning [16, 6] which uses the following update rules for the weights and biases:

$$\begin{aligned}\Delta W_{ij}^0 &\propto \langle \mathbf{v}_i \mathbf{h}_j \rangle_0 - \langle \mathbf{v}_i \mathbf{h}_j \rangle_n \\ \Delta \mathbf{b}_i^0 &\propto \langle \mathbf{v}_i \rangle_0 - \langle \mathbf{v}_i \rangle_n \\ \Delta \mathbf{b}_i^1 &\propto \langle \mathbf{h}_i^1 \rangle_0 - \langle \mathbf{h}_i^1 \rangle_n\end{aligned}$$

where  $\langle \cdot \rangle_n$  denotes the average after assigning the input data to the visible units and performing just  $n$  updates (as in Gibbs sampling) to each layer. Whereas in Gibbs sampling the number of updates required to reach the stationary distribution can be very high, in contrastive divergence learning a very low number of updates is used, usually just 1. Contrastive divergence has been empirically shown to work reasonably well [18]. Bengio's "Learning deep architectures for AI" [4] can be consulted for a tentative explanation of why it works.

### 2.2.2.1 Gaussian-Bernoulli RBM

For some kind of problems with real valued input features, having binary visible units is not an appropriate representation of the data. An option is to normalize the value of the input features to have magnitudes in the range  $[0, 1]$  and use that value as the probability of activation of the unit [4]. However, even this is not an appropriate representation in many cases as the sampling introduces a lot of noise. An alternative that has received a lot of attention in visual and acoustic data modelling is the use of Gaussian-Bernoulli RBMs [2]. In these kind of restricted Boltzmann machines, the value of visible units follows a Gaussian activation probability and the hidden units are normal binary units that follow a Bernoulli distribution.

In order to obtain simpler mathematical equations, the input data to Gaussian-Bernoulli RBMs is usually normalized over the training dataset to have mean 0 and standard deviation 1 for each unit. In that case the energy of a given configuration is:

$$E(\mathbf{v}, \mathbf{h}) = \frac{1}{2}(\mathbf{v} - \mathbf{b})^T(\mathbf{v} - \mathbf{b}) - \mathbf{v}^T W \mathbf{h} - \mathbf{c}^T \mathbf{h}$$

and as in the standard RBM the conditional distribution of  $\mathbf{v}$  given  $\mathbf{h}$  factorizes with expression:

$$P(v_j | \mathbf{h}) \sim \mathcal{N}(-\mathbf{b}_j - W_j \cdot \mathbf{h}, 1)$$

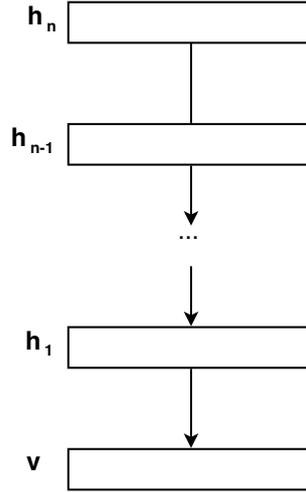


Figure 2.5: Graphical model of a deep belief network.

### 2.2.3 Deep belief networks

A deep belief network (DBN) [18] is a multi-layer generative probabilistic model, made up of stochastic binary units organized in layers. The bottom layer is the visible layer  $\mathbf{v}$ , while the rest of the layers are hidden layers  $\mathbf{h}^1, \mathbf{h}^2, \dots, \mathbf{h}^l$ .

In a DBN the top two layers ( $\mathbf{h}^{l-1}$  and  $\mathbf{h}^l$ ) are connected in an undirected manner and form an RBM. The rest of layers are connected in a top-down directed fashion, see Figure 2.5.

The joint probability of a DBN factorizes as follows:

$$P(\mathbf{v}, \mathbf{h}^1, \mathbf{h}^2, \dots, \mathbf{h}^l) = P(\mathbf{v} | \mathbf{h}^1) P(\mathbf{h}^1 | \mathbf{h}^2) \dots P(\mathbf{h}^{l-2} | \mathbf{h}^{l-1}) P(\mathbf{h}^{l-1}, \mathbf{h}^l)$$

The probability of activation of a unit in any layer below the top two is conditionally independent of the rest of units given the state of the layer directly on top of it, and follows the expression:

$$P(\mathbf{h}_j^i | \mathbf{h}^{i+1}) = \sigma(-\mathbf{b}_j^i - W_j^i \mathbf{h}^{i+1}) \quad (2.3)$$

Therefore, generating samples from a DBN can be achieved by doing Gibbs sampling of the top two layers (i.e. alternately update  $\mathbf{h}^{l-1}$  and  $\mathbf{h}^l$  using equations (2.1) and (2.2) until the stationary distribution is reached). Then, doing ancestral sampling of the lower layers until we reach the visible layer using equation (2.3).

#### 2.2.3.1 Training a deep belief network

The key to successfully train a DBN is to do it in a greedy, layer-wise manner [18]; adding layers on top one at a time.

Initially, a DBN will consist of only 2 layers, the visible and the first hidden layer. These initial two layers are connected in an undirected way (because they are the top two layers), and trained as an RBM.

If a new layer is to be put on top, the connections between the previous top two layers are transformed into directed top-down (directed from the hidden to the visible layer of the RBM) connections. The new layer is added on top, connected to the previous top layer in an undirected fashion. This new top two layers are, again, trained as an RBM. To obtain the visible data of this new RBM, we must get samples from the previous top layer (now visible layer of the top RBM) by running the data examples through the previous layers of the DBN using equation<sup>23</sup>:

$$P(\mathbf{h}_j^l | \mathbf{h}^{l-1}) = \sigma(-\mathbf{b}_j^l - W_{.j}^{l-1T} \mathbf{h}^{l-1})$$

### 2.2.3.2 Using a DBN for regression

As we have seen, a DBN is a generative model, it can not be used directly to perform regression or classification. The purpose of creating a DBN if the aim is doing regression or classification is to create a model capable of representing the visible data at different levels; in the hope that higher layers will contain simpler representations of the data corresponding to higher levels of abstraction. Therefore, obtaining features more useful for the purpose of doing regression or classification. A trained DBN can be easily transformed into such a regression or classification architecture.

There are several ways in which a DBN can be transformed into a classification architecture. In this work, we are only interested in their use for regression. Hinton's "A Practical Guide to Training Restricted Boltzmann Machines" [15] can be consulted if the purpose is classification.

As for regression, even though elaborate methods such as using DBNs to learn covariance kernels for a Gaussian process[50], the simplest option is to transform the DBN into a multilayer neural network [15] by adding a new layer on top that performs linear regression (see Figure 2.6). The DBN weights and biases are used as initial parameter values for the ANN. The top linear regression layer only poses a linear optimization problem and can be trained, for example, using the pseudo-inverse method:

$$\begin{aligned} \mathbf{b}^y &= \bar{\mathbf{y}} \\ W^y &= (\mathbf{h}^n \mathbf{h}^{nT})^{-1} \mathbf{y}^r \end{aligned}$$

Where  $\mathbf{b}^y$  represents the bias of the output layer units,  $\bar{\mathbf{y}}$  the mean of the outputs in the dataset,  $W^y$  the weights from the top hidden layer to the output layer,  $\mathbf{h}^n$  the top hidden

<sup>2</sup>For notational convenience we will denote  $\mathbf{v}$  as  $\mathbf{h}^0$  here.

<sup>3</sup>Usually, the mean-field value is used and no sampling of the binary values is done [15].

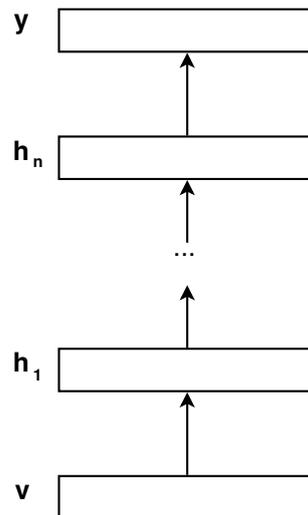


Figure 2.6: DBN transformed into a regression ANN. Output  $y$  is calculated by performing linear regression from the features in  $h_n$ .

layer states for all datapoints in the dataset, and  $y'$  the mean-subtracted outputs in the dataset.

However, performance using the initial weights originated from a DBN, is usually not very good. To improve its performance the model is fine-tuned by performing gradient descent; generally, using the backpropagation algorithm.

Given that the model will have to be fine-tuned anyway, it may seem we have gained nothing from creating the model from a DBN instead of creating an ANN with random initial weights. However, empirical results show that an ANN with more than one or two layers initialised with random weights is usually very difficult to train and tends to get stuck in underperforming local optima. In contrast, ANN initialised with weights from a DBN usually obtain better results [4].

### 2.3 Deep belief networks in phone recognition

In 2009, Mohamed et al. [30] used DBNs to tackle the phone recognition task (i.e. the problem of classifying speech sounds as their corresponding phonemes). Mohamed et al. used as input features 11 frames of 12-th order Mel frequency cepstral coefficients (MFCCs) and energy along with their first and second derivatives. Each frame was analysed using a 25 ms Hamming window and the frame rate was 10 ms. As output labels, 183 classes were used (3 states for each of 61 phonemes), to obtain a probability distribution of the phoneme label for the central frame of acoustic data. These output probability distributions were then fed to a standard Viterbi decoder using a bi-gram model over phonemes.

A standard DBN, with Gaussian units in the visible layer and Bernoulli units in all hidden

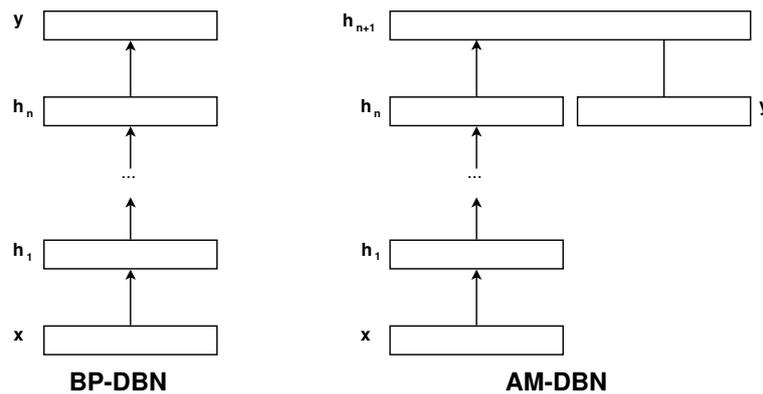


Figure 2.7: BP-DBN on the left and AM-DBN on the right..

layers, was trained on the input data and then transformed into two different types of classification models, which Mohamed et al. denominated BP-DBN and AM-DBN (see Figure 2.7).

The BP-DBN was a standard multi-layer neural network initialised with the DBN weights and a layer of softmax units added on top. The model was fine-tuned using backpropagation.

The AM-DBN architecture was also a standard multi-layer neural network initialised with the DBN weights, but with an RBM added on top that models the joint distribution of the top level features and the output labels, acting as an associative memory. This model also requires fine-tuning using backpropagation.

Mohamed et al. trained both models on the TIMIT dataset using a variety of number of layers and units per layer. They found a BP-DBN trained using 4 hidden layers of 2048 units plus a narrow second to last layer of 128 units offered best results, with a PER (phone error rate) of 23.00%, which they claimed as better than all other techniques tried on this dataset. The best AM-DBN offered a PER of 23.85% using 3 hidden layers of 3072 units each.

In conclusion, the authors found that using a deep architecture of 4 hidden layers trained in an unsupervised manner and fine-tuned using backpropagation is a viable approach to phone recognition, able to beat previous state-of-the-art methods.

In 2010 Dahl et al. [10] extended Mohamed's previous work by substituting the first layer of the DBN with a mean-covariance RBM (mc-RBM). Dahl et al. argue that a Gaussian RBM (the model used for Mohamed's previous work first layer) has representational deficiencies. The state of the visible units in a Gaussian RBM are conditionally independent of each other given the hidden output. A deficiency they compare to having diagonal covariance matrices in a Gaussian Mixture Model.

Trying to ameliorate this deficiency, they use a mean-covariance RBM [41] for the first

layer of their system. A mean-covariance RBM is made-up of a set of Gaussian units (also called mean units) and another set of units called the precision units. The precision units form a third order Boltzmann machine, and define a sample-specific covariance matrix by capturing multiplicative interactions between two visible units and one precision unit.

The output of this mc-RBM was used as the input to a DBN. No backpropagation is done to the mc-RBM when the system is transformed into an ANN after unsupervised training.

The acoustic features used as input in this paper differ from Mohamed's previous work: 15 acoustic frames each formed by 39 Mel scale filterbank coefficients and 1 energy log magnitudes were concatenated and PCA whitening applied, after which only the 384 most important components were used as inputs. Of special relevance is the absence of delta features, which purportedly are not needed when using an mc-RBM.

Best results, measured on the TIMIT test dataset, were achieved using 1024 precision units and 512 mean units for the mc-RBM, and 8 more hidden layers of 2048 units each; obtaining a phone error rate of 21.7%.

Dahl et al. report training a system equivalent to that of Mohamed's previous work but with an mc-RBM as the first layer in order to "isolate the advantage of using an mc-RBM instead of a Gaussian-RBM" from the improvement due to the new kind of inputs. They obtained a phone error rate of 22.3% (a 1.4% improvement with respect to Mohamed's work). However no details about the configuration are reported in the paper. Of special interest would be whether they utilized delta features as inputs, as they consider the ability of the mc-RBM to "extract its own useful features that make explicit inclusion of difference features unnecessary" the main advantage of its use. Therefore, if they were not used, the improvement would be more indicative of the advantage of using first layer an mc-RBM instead of a Gaussian-RBM for the first layer.

It must be kept in mind that Dahl et al. report that using an mc-RBM more than doubled the training time of the system. Dahl et al. have abandoned the use of mc-RBM in their more recent publications. Whether this is because their accuracy improvement disappears when adding other modifications or because they result impractical due to their long training times has not been specified.

In 2011, Mohamed et al. published [31] a review of their previous work. In this paper they introduce the use of filterbank coefficients augmented with delta and delta-delta features (a simpler representation than Mel frequency cepstral coefficients). They obtain a phone error rate of 20.7% on the TIMIT test dataset, and conclude that a deep architecture is able to extract better features out of these less processed input features.

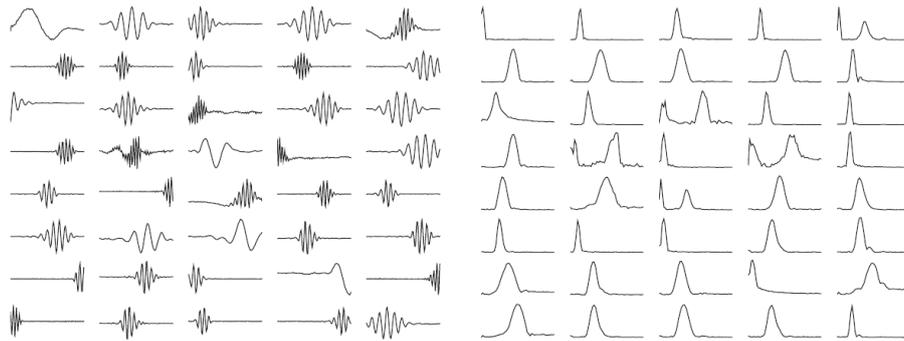


Figure 2.8: On the left forty random features learned by the first layer RBM in Jaitly and Hinton [22] (each feature is shown by plotting the connection weights from a hidden unit to all visible units). On the right the Fourier transform of the features. (Image reproduced from [22] with the author's permission)

In 2011, Mohamed et al. [32] published an extension of Mohamed's previous work. In this work, they compare their previous results using Mel frequency cepstral coefficients with three modifications: (1) the use of a vector of 40 linear discriminant analysis features (LDA), (2) the combination of LDA features using speaker adaptation by vocal tract length normalisation, and (3) the addition of discriminative features trained using the boosted maximum mutual information criterion [37].

As in previous papers, the performance is measured on the test TIMIT dataset. Raw LDA features were found to offer no accuracy improvement. However, both speaker adaptation and discriminative features offered improved results. A 4 hidden-layer ANN pretrained as a DBN, with 1024 units per hidden layer using as inputs LDA features after speaker adaptations obtained a phone recognition error of 20.3%. Adding discriminative features reduced the error even further to 19.6%.

In 2011, Jaitly and Hinton [22] introduced the use of a specialized type of RBMs to model speech data directly from the raw acoustic signal, instead of using a low dimensional encoding as filterbank coefficients, Mel cepstrum coefficients or linear predictive coding.

In their work, Jaitly and Hinton, use as the first layer of their system an RBM that has Gaussian visible units and rectified linear hidden units (RLU). The value of a rectified linear unit is  $\max(0, N(x, \sigma(x)))$  where  $x$  represents the input to the unit. This kind of units were first used by Nair and Hinton and are reported to improve the performance of DBN based systems in comparison with other kinds of continuously valued hidden units (like for example Gaussian units).

Jaitly and Hinton, trained this kind of RBM on the TIMIT development dataset raw input signal and found it captured features like those shown in Figure 2.8.

Finally, they trained a standard 3 hidden layers (4000 units each) DBN using these features as input, and use it for phone recognition using 183 states as in Mohamed's work. They obtain a phone error rate on the TIMIT test dataset of 21.8%. A remarkable result given that they use the raw acoustic signal as input.

The good results obtained by deep belief network systems in phone recognition led us to hypothesise they could be a good system for articulatory inversion. The similarity is obvious, both problems process acoustic speech signals. However, there is a very important difference between both: phone recognition is a classification problem, while articulatory inversion is a regression problem.

## Chapter 3

# Data and Evaluation Criteria

### 3.1 The MNGU0 dataset

Although the FSEW0 dataset (part of the MOCHA-TIMIT corpus [55]) has been the electromagnetic midsagittal articuography dataset most widely used in previous articulatory inversion research, in this dissertation we have opted for using the recently introduced MNGU0 dataset [47]. Our preference for the MNGU0 dataset is based on several issues concerning the quality of the MOCHA-TIMIT EMA measurements.

MOCHA-TIMIT is an older dataset and was recorded using a Cartsens AG200 electromagnetic articuograph. This articuograph consists of only 3 fixed transmitter coils. These make it possible to measure the position of the transducer coils only on a 2-dimensional plane. Therefore, movement of the head during a EMA recording session or rotation of the transducer coils due to articulator movement can have a negative impact on the precision of the measurements. Moreover, during the recording of the MOCHA-TIMIT fsew0 dataset, a coil became detached and had to be re-attached; since it is impossible to attach it at exactly the same position, inevitably this also added a certain degree of inconsistency to the dataset.

In contrast, the MNGU0 [46] dataset was recorded using a more modern Cartsens AG500 electromagnetic articuograph. This newer model consists of 6 transmitter coils, which make it possible to track the position of the transducer coils in three dimensions along with two angles of rotation. This makes movement of the head during the EMA session irrelevant, as the articulator positions are calculated relative to the position of other reference coils placed on the skull. Moreover, no coil became detached during the recording of the MNGU0 dataset.

To show that the MNGU0 dataset has a higher level of precision than the FSEW0 dataset, Richmond [46] measured the accuracy of his trajectory mixture density network articulatory inversion system on both, obtaining an RMSE of 1.54mm for FSEW0 and 0.99mm for

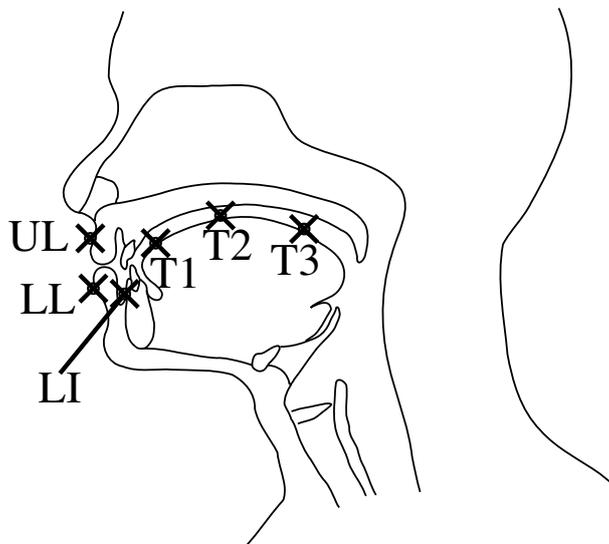


Figure 3.1: Midsagittal plane figure showing the positioning of electromagnetic coils for vocal tract articulator tracking in the MNGU0 dataset. The articulators tracked are: upper lip (UL), lower lip (LL), lower incisor (LI), tongue tip (T1), tongue blade (T2), and tongue dorsum (T3). Image courtesy of Korin Richmond.

MNGU0.

### 3.1.1 Data setup

The MNGU0 EMA dataset used in this dissertation, consists of 1263 utterances recorded from a single speaker in a single session. Parallel recordings of acoustic data and the position of 6 coils is available. Transducer coils were placed in the midsagittal plane at the upper lip, lower lip, lower incisors, tongue tip, tongue blade and tongue dorsum (see Figure 3.1).

Although MNGU0 EMA data consists of 3-dimensional measurements, only movement in the midsagittal plane (therefore 2-dimensional) was considered. The reason for this is twofold, movement perpendicular to the midsagittal plane was very small, and it eases comparison with results from previous research by Richmond [46].

Each EMA data frame is made up by 12 coordinates, two ( $x$  and  $y$  position) for each articulator tracked, with a sampling frequency of 200 Hz. The acoustic data consists on frames of 40 frequency warped line spectral frequencies (LSFs) [52] and a gain value, the frame shift step is 5 ms in order to obtain acoustic features at the same frequency as the EMA data.

In our experiments we will use the same data setup as Richmond in [46]. As input, we use a context window of 10 acoustic frames selecting only every other frame. Therefore, each input window will span a period of 100 ms. As output, we will use the EMA frame that corresponds to the time at the middle of the current acoustic window, i.e. between acoustic

frames 5 and 6.

The dataset is partitioned in three sets: a validation and a training set comprising 63 utterances each, and a training set consisting of the other 1137 utterances.

## 3.2 Evaluation criteria

In this work, we will use two metrics to measure the accuracy of our system:

- The root mean-squared error (RMSE), this is the most widely used measure of an articulatory inversion system performance, and is defined as

$$RMSE = \sqrt{\frac{1}{N} \sum_i (e_i - t_i)^2}$$

where  $e_i$  is the estimated tract variable and  $t_i$  the actual tract variable at time  $i$ .

- The correlation with the actual articulator trajectories, defined as

$$r = \frac{\sum_i (e_i - \bar{e})(t_i - \bar{t})}{\sqrt{\sum_i (e_i - \bar{e})^2 \sum_i (t_i - \bar{t})^2}}$$

where  $\bar{e}$  is the mean value of the estimated tract variable,  $\bar{t}$  the mean value of the actual tract variable.

A good articulatory inversion system must obtain low RMSE and high correlation with respect to real articulatory data.

We will focus on the root mean-squared error as it is the most widely reported measure of articulatory inversion accuracy and is the only measure for which we have previous results on the MNGU0 dataset. However, we will also report the correlation of the most important results.

## 3.3 Benchmarks

In order to judge the relevance of our results, we need to set some reference points with which we can compare them using the test set of the MNGU0 dataset.

A linear model that uses as input a window of acoustic data and as output a frame of articulatory data, obtains an average RMSE of 1.52 mm. This result gives us an idea of what can be achieved with a very simple model. Any RMSE greater than that would indicate our system is obtaining very bad results.

A regular one-hidden-layer artificial neural network with 300 units, obtains an average RMSE of about 1.13 mm. this sets a benchmark for a simple model but one not so naive as a linear model.

Then we can set some reference points for what would be state-of-the-art accuracies. Richmond's trajectory mixture density networks<sup>1</sup> obtain when using one Gaussian-mixture per articulatory channel an average RMSE of 1.03 mm. When using 1,2 or 4 Gaussian-mixtures (the number is optimized for each channel) the average RMSE shrinks to 0.99 mm [46]. Recently, Richmond's trajectory mixture density network have obtained a new, still unpublished, record accuracy of 0.96 mm RMSE [43].

We cannot know how much variability is due to measurement error of the EMA machine. Moreover, because not all articulators are equally relevant in the production of a given sound [35], a slight change of position of some of them will not affect the sound produced much, this also introduces a certain degree of variability in the articulatory data that is inherent to the speech production process and cannot be avoided. Therefore, it is impossible for us to know what is the smallest RMS error achievable.

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<sup>1</sup>We consider Richmond's TMDN as the state-of-the-art given that he obtains the best accuracies on the MOCHA-TIMIT, which is the most widely tried EMA dataset. Fortunately, we also have results for the novel MNGU0 dataset.

## Chapter 4

# Implementation and Results

Motivated by their good performance in phone recognition, we introduce in this dissertation a deep belief network for articulatory inversion.

Given that the process of training restricted Boltzmann machines is computationally expensive, we designed our system to take advantage of the computational speed-up provided by GP-GPU (general purpose computation on graphics processing units). In our implementation we used the matrix algebra CUDAMat Python library [29]. We obtained approximately 5 times shorter RBM training times and 2.5 times shorter backpropagation times compared to using 6 CPUs. More details about our specific hardware configuration and training times can be found in Appendix A.

### 4.1 A deep belief network for articulatory inversion

#### 4.1.1 Pretraining

To create our articulatory inversion system, first we trained a deep belief network to model speech acoustic data<sup>1</sup>. Given that acoustic data is not binary, but continuous, we used a Gaussian-Bernoulli restricted Boltzmann machine (see page 13) for the first layer of our DBN. To train it we used the contrastive divergence criterion using, as it is common, just 1 sampling step<sup>2</sup> (CD1).

The final training configuration parameters are shown in table 4.1, and were the result of manually tuning them to obtain a low reconstruction error. The heuristics in Hinton’s “A

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<sup>1</sup>To be more precise speech acoustic data produced by the speaker in the MNGU0 dataset.

<sup>2</sup>A better generative model is usually obtained using a higher number of sampling steps [4]. However, it is considered not worth it to use a higher number of steps [15] when the model is going to be transformed into an artificial neural network and fine-tuned with backpropagation.

Parameter	Value
Learning rate	0.00001
Momentum	0.5 (10 first epochs) 0.9 (rest of epochs)
Total epochs	200
Minibatch size	100
Initial weights	$\mathcal{N}(0, 0.01)$
Initial visible bias	0
Initial hidden bias	-4
Weight decay	0.0001

Table 4.1: Training configuration for the Gaussian-Bernoulli RBM used as the first layer of the articulatory inversion DBN.

practical guide to training restricted Boltzmann machines” [15] were of great help in this endeavour.

Figure 4.1 shows some of the receptive fields learned by sixty hidden units of the Gaussian-Bernoulli RBM.

We can observe some of them show blobs of high or low activation (light and dark regions respectively), this blobs capture continuity patterns of the acoustic data in the time and frequency domains. Four examples can be seen in Figure 4.2 on page 28.

Some other units, display vertical patterns of high activity flanked by low activity (light vertical lines flanked by dark vertical lines) and usually occupy the whole frequency (vertical) spectrum. These features capture activation contrasts between contiguous acoustic frames. Four examples can be seen in Figure 4.3.

We tried different sizes for the hidden layer of the Gaussian-Bernoulli RBM. We found that the final average reconstruction error decreases as the number of hidden units is increased, but saturates at 300 units and does not improve by adding more hidden units after that.

More layers were trained on top by following the conventional procedure for DBNs: freezing the weights of the layer just trained and using its hidden layer activation probabilities as input for the new layer. In these higher layers both visible and hidden units take binary values<sup>3</sup> and are therefore Bernoulli-Bernoulli RBMs. The training configuration for the higher layers is shown in Table 4.2 on page 29.

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<sup>3</sup>However, no sampling is performed of the input, it is the activation probability that is used as input for the new visible layer.

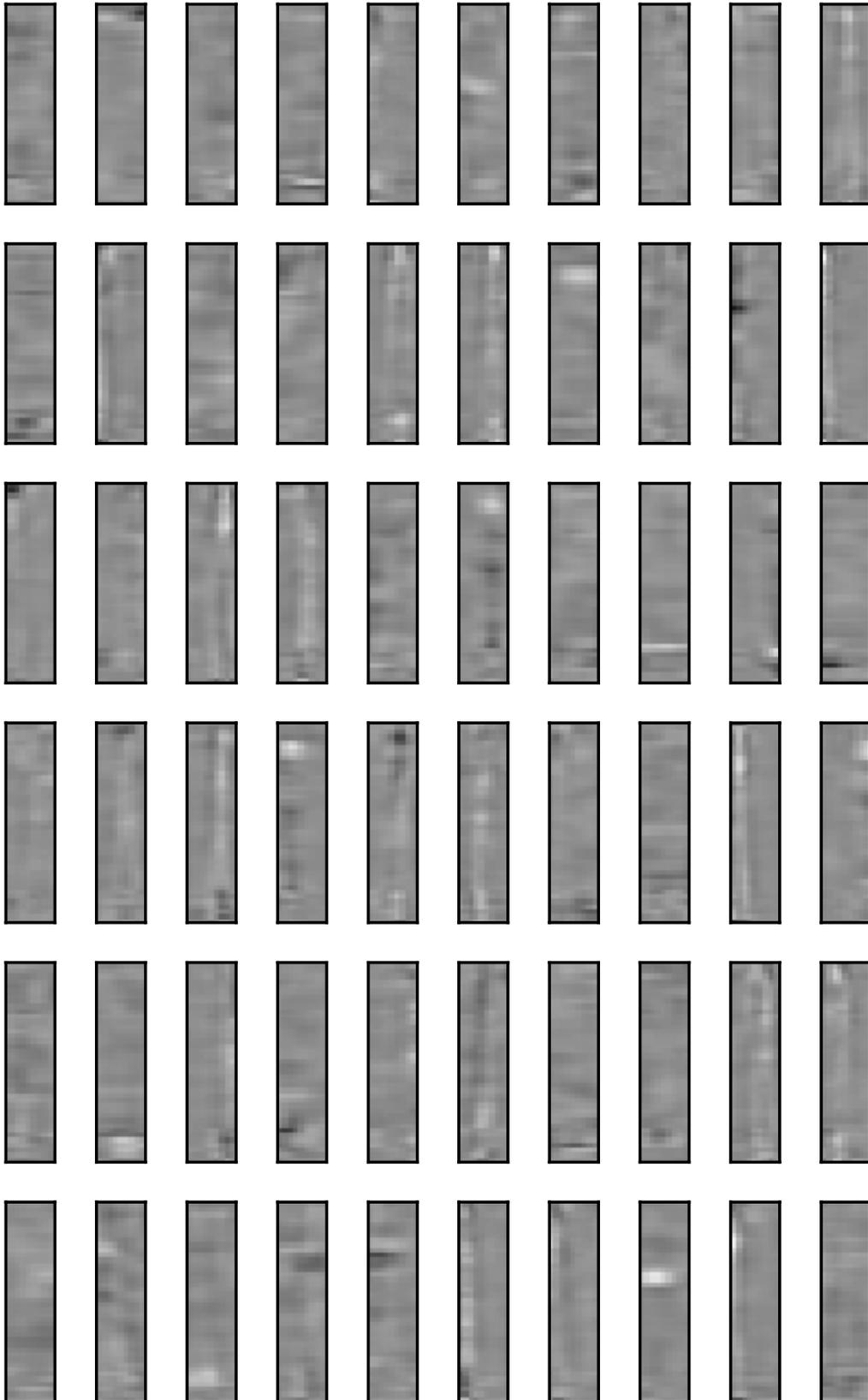


Figure 4.1: Receptive fields of the first 60 units (in this experiment the hidden layer had a total of 300 hidden units) of a Gaussian-Bernoulli RBM trained as the first layer of our DBN. Each receptive field is displayed by plotting the connection weight to each of the 410 visible units. Each column in a field connects to each of the ten acoustic frames used as input. Each point in a column shows a LSF coefficient (lower frequencies at the top) and the gain appears at the bottom.

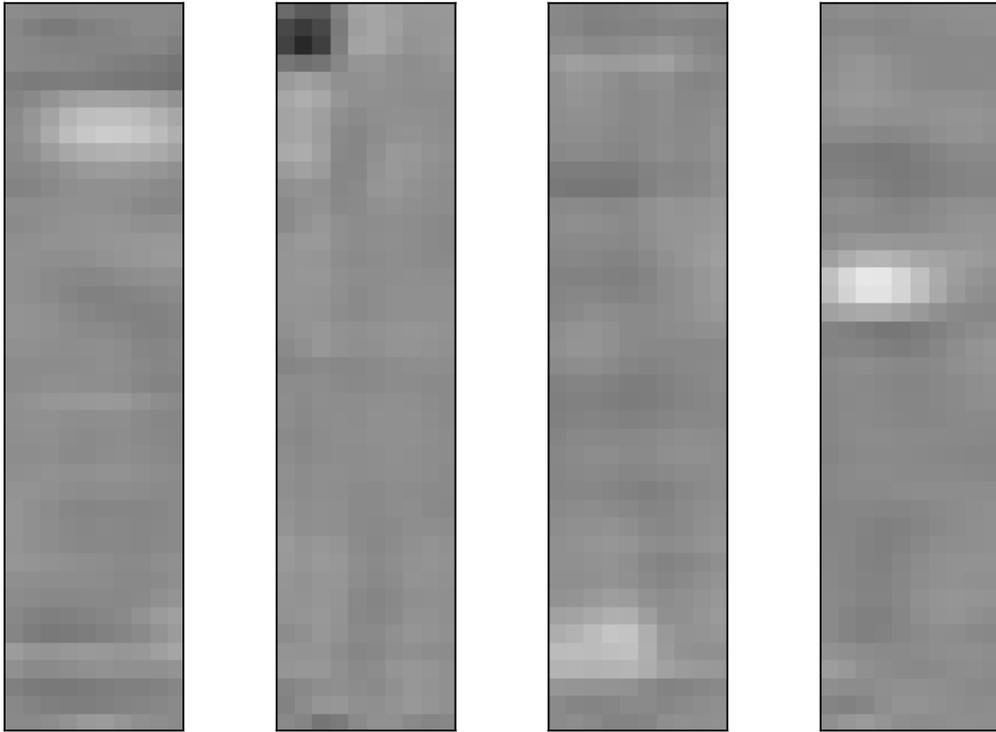


Figure 4.2: Receptive fields of four hidden units that capture blob-like patterns.

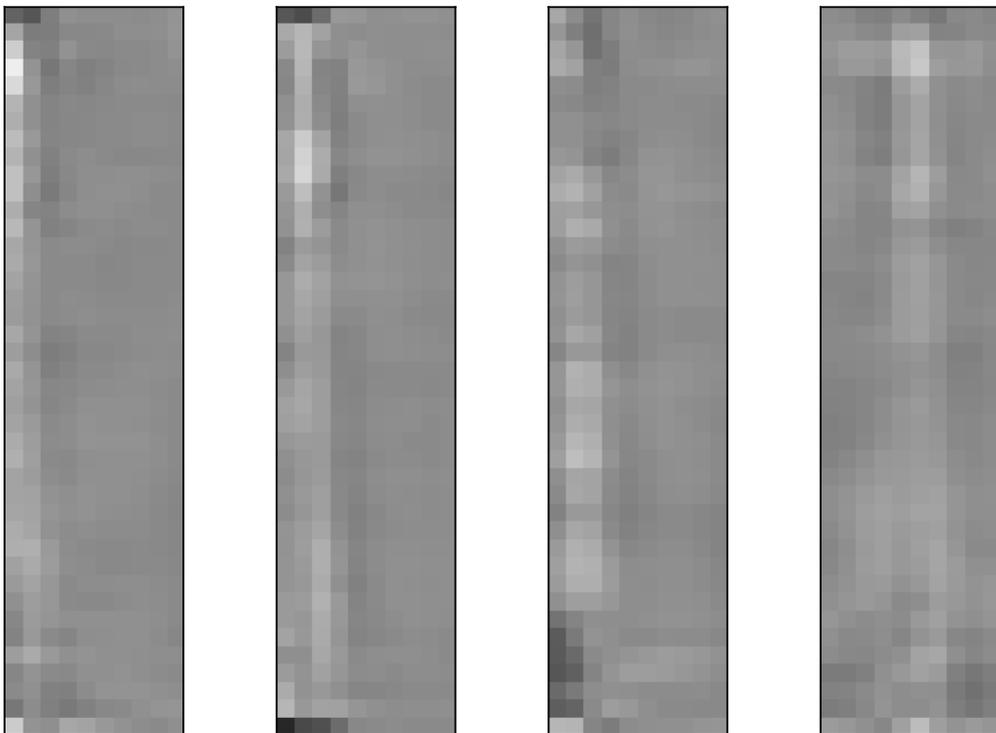


Figure 4.3: Receptive fields of four hidden units that capture column-like patterns.

Parameter	Value
Learning rate	0.0001
Momentum	0.5 (10 first epochs) 0.9 (rest of epochs)
Total epochs	200
Minibatch size	100
Initial weights	$\mathcal{N}(0, 0.01)$
Initial visible bias	0
Initial hidden bias	-4
Weight decay	0.0001

Table 4.2: Training configuration for the Bernoulli-Bernoulli RBMs used for all layers of the articulatory inversion DBN except the first.

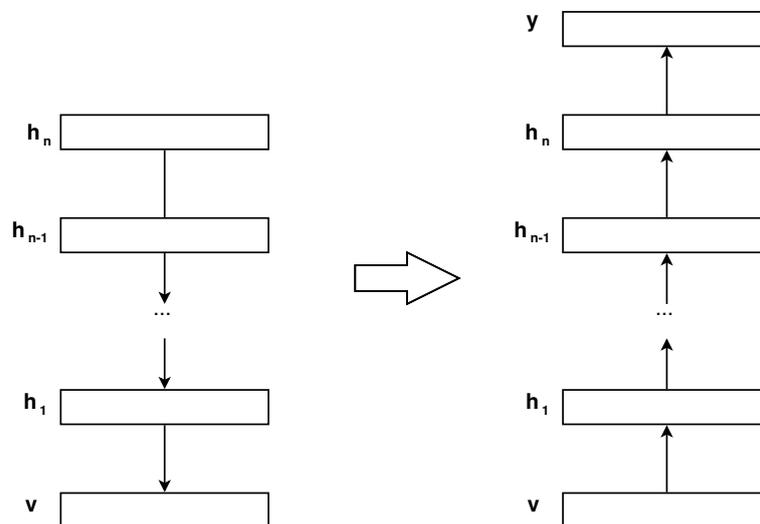


Figure 4.4: Transformation of a deep belief network into a regression artificial neural network by adding a regression layer on top.

#### 4.1.2 Adaptation of the DBN for articulatory regression

In order to adapt the deep belief network (DBN) trained to do regression of the articulator positions, we transformed the DBN into an artificial neural network (ANN), by using the DBN generative weights as the initial weights of the ANN, and adding a linear regression layer on top with one output unit per articulatory channel we want to infer (see Figure 4.4).

To train this ANN, we first trained the top regression layer by using the pseudo-inverse method, as this is just a linear regression problem. Then we performed backpropagation as in a regular artificial neural network to fine-tune the features captured by the hidden layers and the top-layer linear regression weights. The reason why we train the top layer before doing backpropagation is that if we did not, the backpropagation procedure would break our pretrained features in the hidden layers by backpropagating big error gradients due to

Parameter	Value
Learning rate	0.0001
Momentum	0.5 (10 first epochs) 0.9 (rest of epochs)
Total epochs	150
Minibatch size	100
Weight decay	0.0001

Table 4.3: Training configuration of the backpropagation phase.

	200 units	300 units	400 units	500 units
1 hidden layer	1.1063	1.0787	1.0791	1.0656
2 hidden layers	1.0433	1.0350	1.0406	1.0470
3 hidden layers	1.0399	<b>1.0258</b>	1.0330	1.0542
4 hidden layers	1.0631	1.0395	1.0767	1.0602

Table 4.4: RMSE performance of ANNs pretrained as DBNs on the MNGU0 test dataset as a function of the number of hidden layers and the number of units per layer.

poor initialization of the top layer.

The training configuration of the backpropagation phase can be seen in Table 4.3.

### 4.1.3 Results

Using the procedure explained in the two previous sections, we trained a variety of DBNs with different numbers of layers and units per layer using the training set from the MNGU0 dataset. Their performance on the test set of the MNGU0 dataset using the root mean square error (RMSE) criterion is shown in Table 4.4 and Figure 4.5 on page 32. Figure 4.5 on page 32 also shows two dashed horizontal lines with the performance of Richmond's [46] trajectory mixture density network using one-Gaussian mixture or up to four (varying for each articulator channel) Gaussian mixtures.

We can observe that the best results are obtained using 3 hidden layers and 300 units per hidden layer, with an average RMS error of 1.026 mm and average correlation of 0.87 with the real articulator trajectories. A detailed report of the RMSE and correlation per articulator can be found in Table 4.5.

This simple deep architecture performs regression from one window of acoustic data to one frame of articulatory output with no regard for the continuity or dynamical properties of the articulator trajectories. Therefore, it is quite remarkable that it is able to beat a one-Gaussian-mixture trajectory mixture density network, which takes into account the

	RMSE (mm)	Correlation
T3 x	1.229	0.859
T3 y	1.658	0.887
T2 x	1.375	0.855
T2 y	1.304	0.932
T1 x	1.338	0.895
T1 y	1.345	0.919
JAW x	0.632	0.798
JAW y	0.757	0.905
UL x	0.347	0.818
UL y	0.488	0.813
UL x	0.699	0.855
UL y	1.136	0.896
Average	<b>1.026</b>	<b>0.8695</b>

Table 4.5: Per articulator RMSE and correlation performance on the MNGU0 test dataset of a 3 hidden layer ANN with 300 units per hidden layer, pretrained as a DBN.

dynamic constraints of the articulatory data by using delta and delta-delta output features to infer the most probable trajectory of the articulators using maximum-likelihood parameter generation.

Our results suggest that a deep architecture can obtain better results than a shallow 1-hidden layer system. However, it could be argued that is the use of a greater number of parameters and not the hidden layers that matters. To test that possibility, in Figure 4.6 on page 33 we plot the RMSE of each ANN versus its number of tunable parameters. We can observe that a 3 hidden-layers architecture is superior to shallower architectures even when using the same number or even fewer tunable parameters. Therefore, we conclude a deep architecture works better than a shallow one to perform articulatory inversion.

To check whether we could have achieved similar results without the DBN pretraining phase, we trained a set of randomly initialised artificial neural networks. The results are shown in Figure 4.7 on page 34. We can observe that in all cases a ANN pretrained as a DBN obtains better results than a randomly initialized ANN. However, in contrast to what is usually posited in the deep architecture literature, we found no trouble in training 2 and 3 hidden-layer ANNs with randomly initialised weights, and they showed improvement compared to shallower architectures. Even though, the results were in fact inferior to pretrained models.

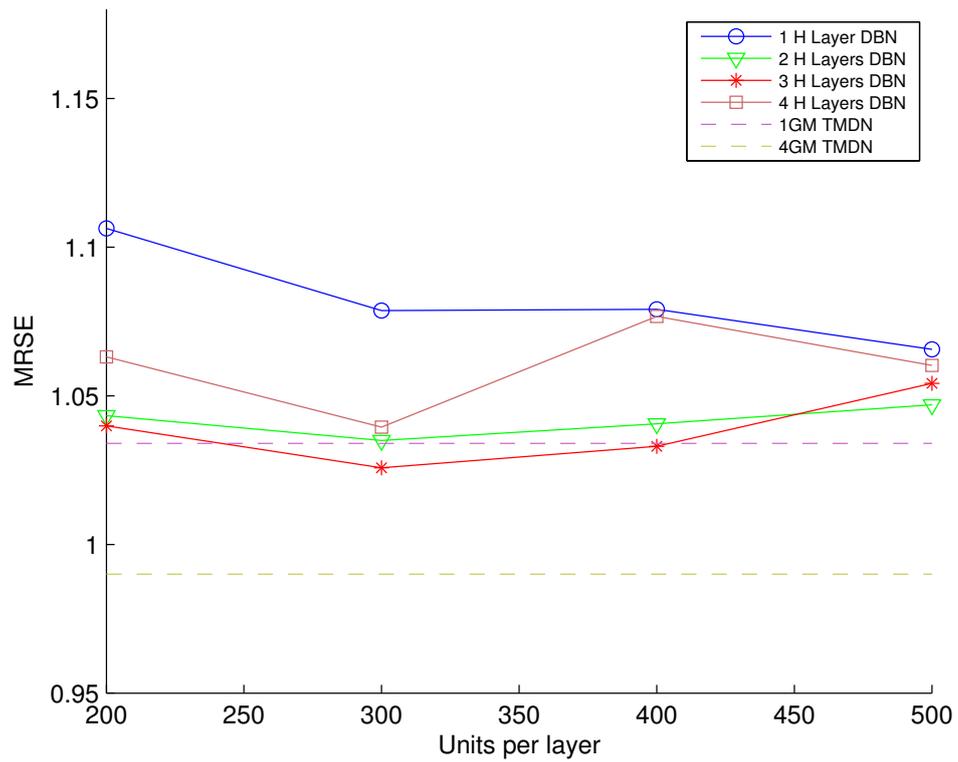


Figure 4.5: RMSE performance of ANNs pretrained as DBNs on the MNGU0 test dataset as a function of the number of units per layer. Four series are shown, using 1,2,3 and 4 hidden layers respectively. As reference, the accuracies of a 1GM TMDN and 4GM TMDN are also shown.

Best results are obtained using a 3 hidden layers DBN with 300 units per hidden layer.

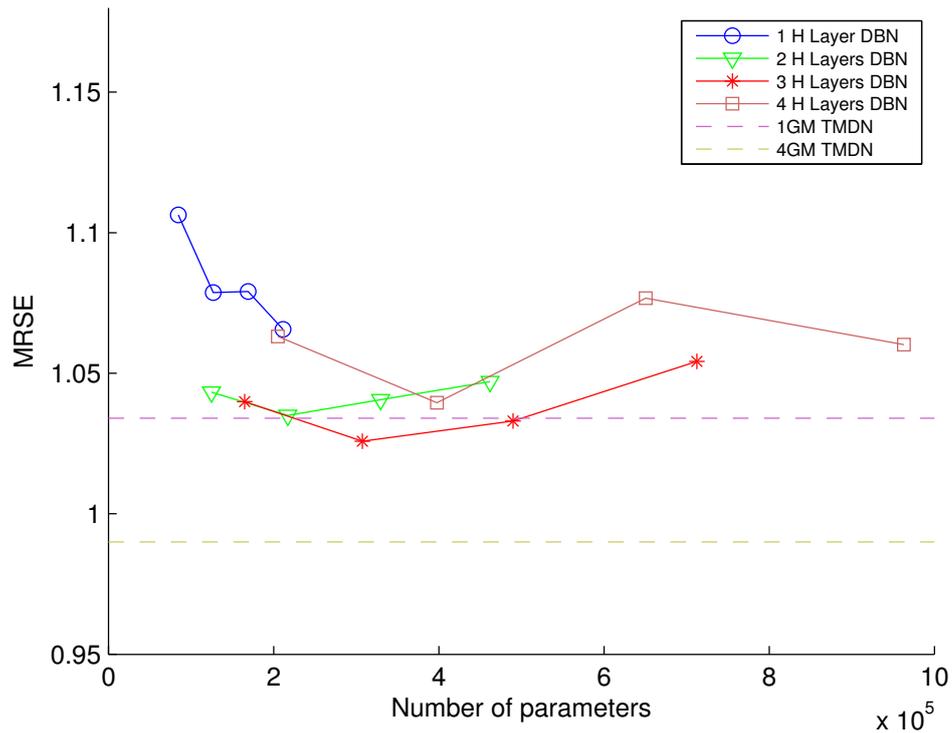


Figure 4.6: RMSE performance of ANNs pre-trained as DBNs on the MNGU0 test dataset as a function of the number of tunable parameters in the system. Four series are shown, using 1,2,3 and 4 hidden layers respectively, each showing a data-point at 200, 300, 400 and 500 units per hidden layer. As reference, the accuracies of a 1GM TMDN and 4GM TMDN are also shown.

A 3 hidden layer DBN obtains better results than 1 or 2 hidden layer DBNs even when using the same number or fewer tunable parameters.

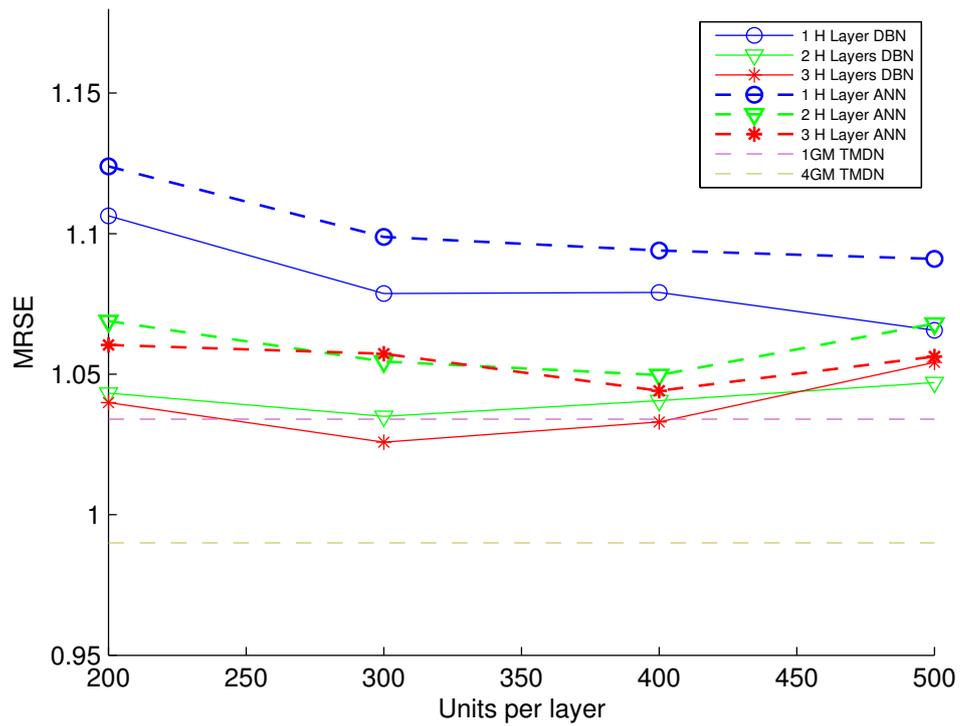


Figure 4.7: Comparison of RMSE performance on the MNGU0 test dataset between ANNs pretrained as DBNs, and ANNs initialised randomly. Six series are shown, using 1,2,3 hidden layers respectively for each kind of ANN. As reference, the accuracies of a 1GM TMDN and 4GM TMDN are also shown.

ANNs pretrained as DBNs always beat randomly initialised ANNs.

T3 x	T3 y	T2 x	T2 y	T1 x	T1 y	JAW x	JAW y	UL x	UL y	LL x	LL y
7 Hz	6 Hz	7 Hz	8 Hz	7 Hz	9 Hz	6 Hz	9 Hz	6 Hz	6 Hz	7 Hz	10 Hz

Table 4.6: List of optimal integer cut-off frequency for each articulator channel

## 4.2 Low-pass filtering

So far in our system each frame of articulatory data is inferred from a window of acoustic data with no regard for the fact that the articulatory data forms a time series and will have some dynamical characteristics. In Richmond's recent work, dynamical constraints are added by inferring delta and delta-delta (velocity and acceleration) features along with the static estimation of the articulator's position. Using these static and dynamic features Richmond runs a maximum likelihood parameter generation (MLPG) that infers the most likely trajectory in conformance with the dynamic constraints [45]. Unfortunately, the MLPG algorithm requires probability distributions of the static and dynamic features, not point estimations, and due to the limited time we had for this dissertation, we considered it out of reach.

In order to account for the dynamic nature of articulatory data in a simpler manner, we can take the approach followed by Richmond in his earlier work. In his doctoral dissertation, Richmond noticed the output of his articulatory inversion system based on artificial neural networks had a higher variability (higher frequency components) than real articulatory data. To eliminate the higher frequency components of his output, Richmond applied a low-pass filter obtaining as a result articulatory trajectory estimations with a lower root mean square error and higher correlation.

If we plot the output of our system, for example for the first utterance in the MNGU0 test set as shown in Figure 4.8 on the following page, we can observe our output also has high frequency components that appear absent in the real articulatory data.

Using the same approach as Richmond, we apply a zero-shift second order Butterworth low-pass filter to our output. The movement of different articulators can have different dynamical characteristics. Therefore, in order to decide the cut-off frequency to use for each articulator channel we calculated the RMSE on the MNGU0 training dataset using integer cut-off frequencies in the range 1-20 Hz for each channel and choose the optimal for each of them. We obtained the cut-off frequencies shown in Table 4.6.

After low-pass filtering the output of our system, we can observe (see Figure 4.10 on page 38) by visual inspection that the output of our system resembles the real articulatory data more accurately than previously. The improvement is also reflected into lower RMSE values, shown in Table 4.7 and plotted in Figure 4.9.

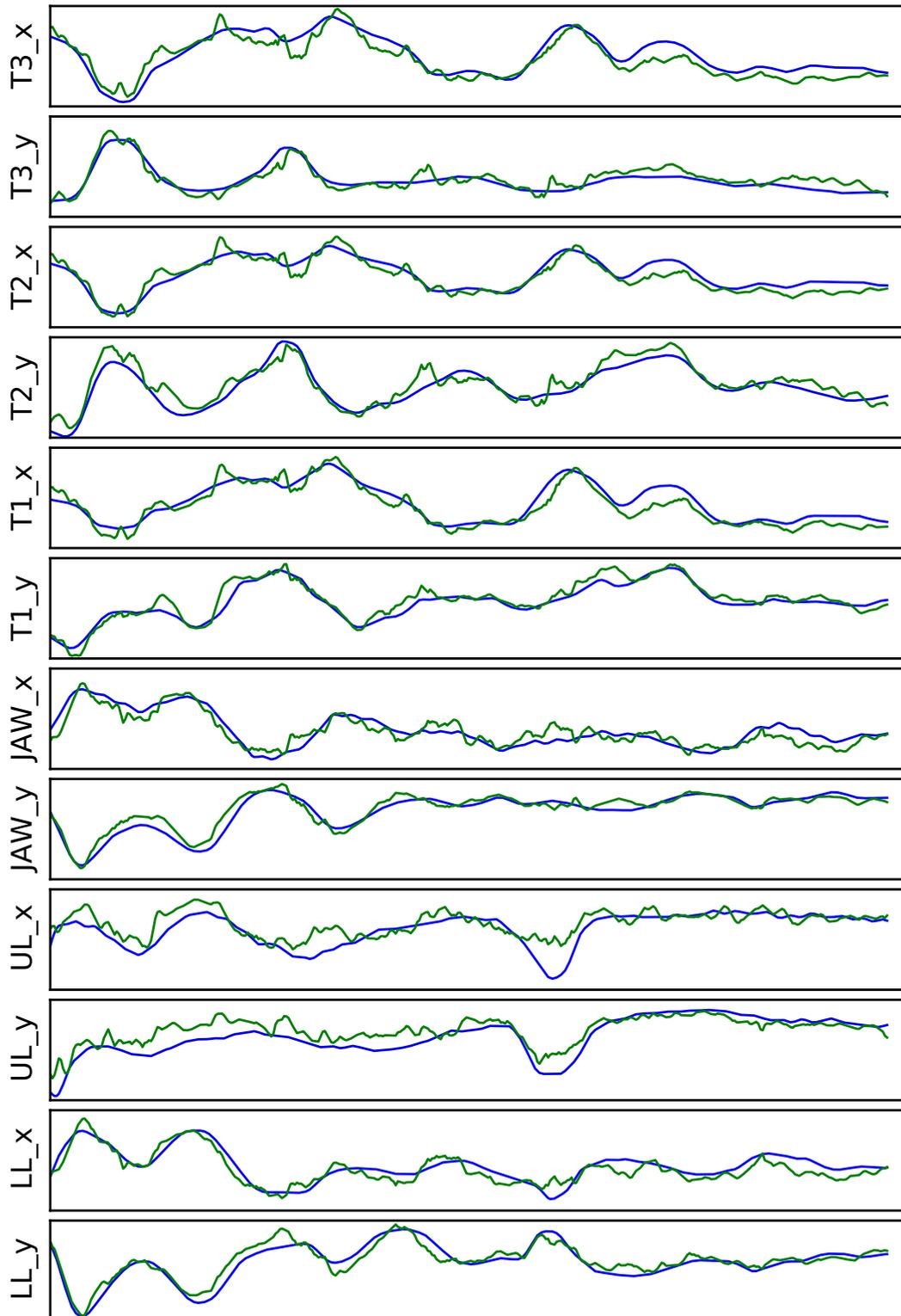


Figure 4.8: Real and inferred articulator trajectories for the first utterance of the MNGU0 test set. The real trajectory is shown in blue, the inferred trajectory in green.

	200 units	300 units	400 units	500 units
1 hidden layer	1.0446	1.0174	1.0171	1.0010
2 hidden layers	0.9876	0.9711	0.9729	0.9707
3 hidden layers	0.9786	<b>0.9544</b>	0.9639	0.9841

Table 4.7: RMSE performance of ANNs pretrained as DBNs on the MNGU0 test dataset as a function of the number of hidden layers and the number of units per layer.

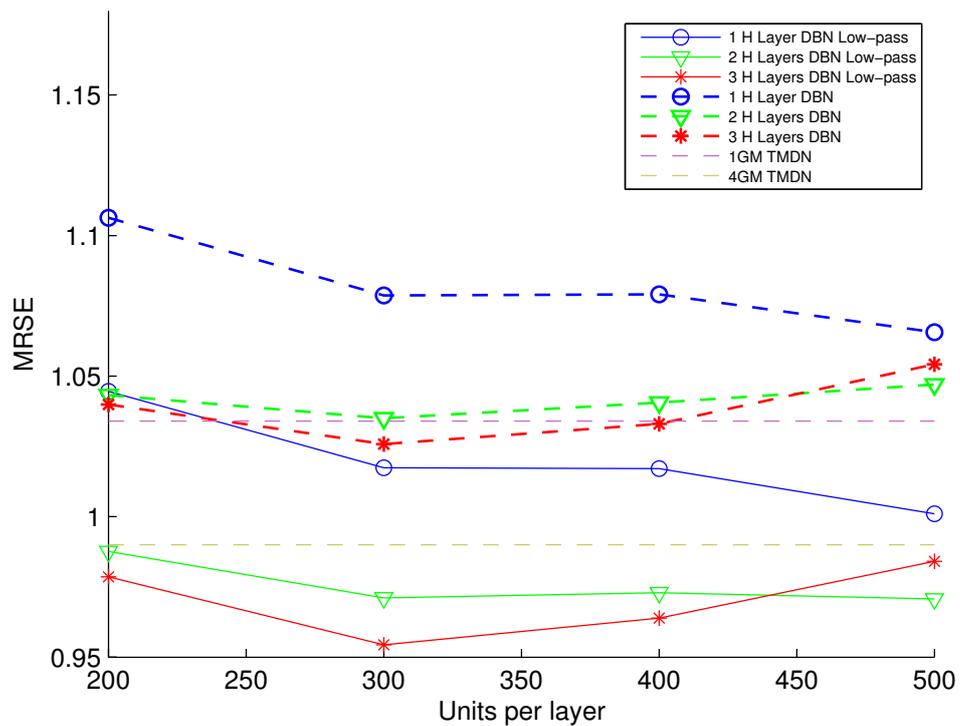


Figure 4.9: RMSE performance of ANNs pretrained as DBNs on the MNGU0 test dataset as a function of the number of units per layer. Six series are shown, using 1,2,3 hidden layers, with the accuracies of low-passed filtered trajectories shown as solid lines, and unfiltered output accuracies as dashed lines. As reference, the accuracies of a 1GM TMDN and 4GM TMDN are also shown.

Best results are obtained using a 3 hidden layers DBN with 300 units per hidden layer.

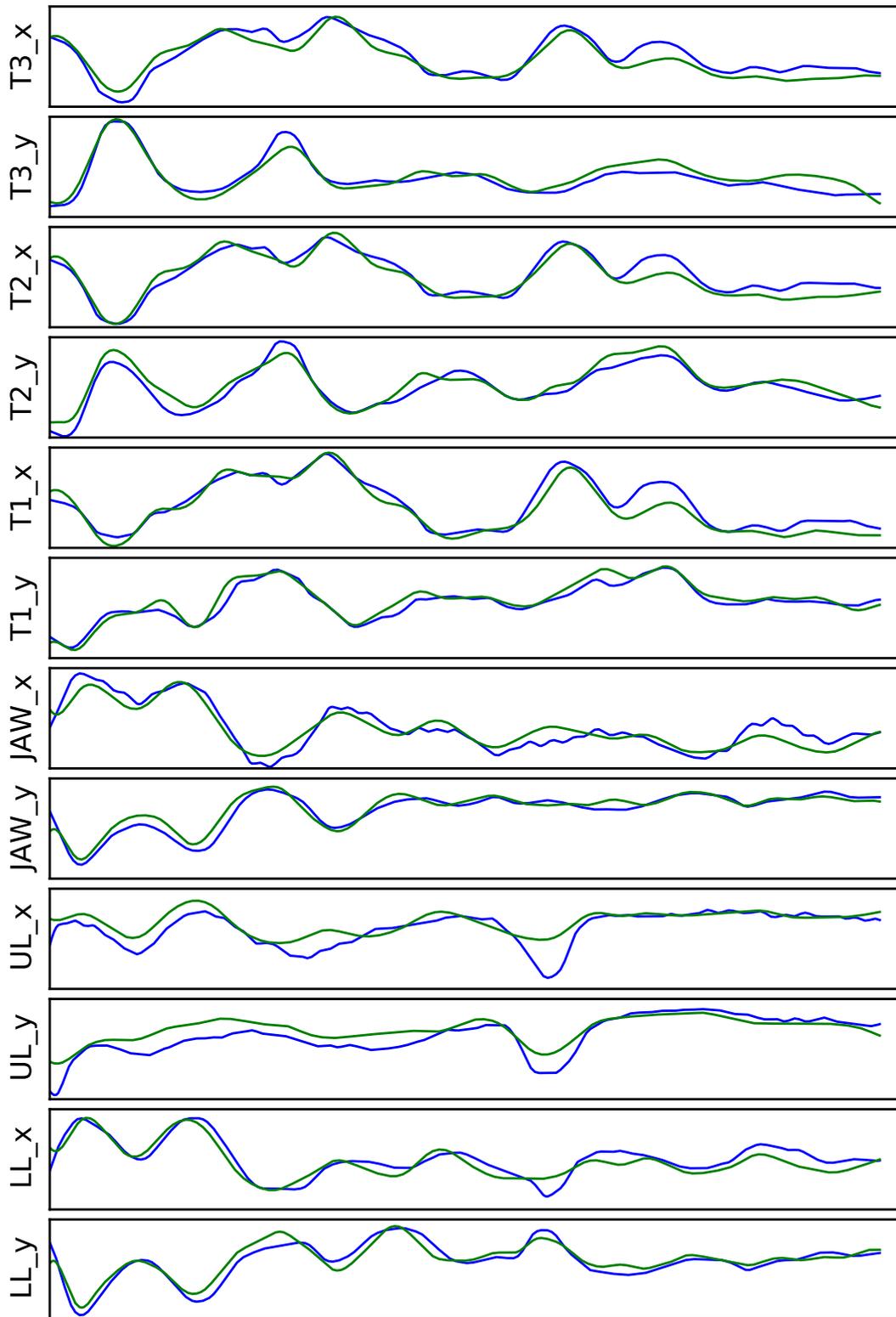


Figure 4.10: Real and inferred articulator trajectories for the first utterance of the MNGU0 test set. The inferred trajectory has been low-pass filtered using the cut-off frequencies shown in Table 4.6. The real trajectory is shown in blue, the inferred trajectory in green.

	RMSE (mm)	Correlation
T3 x	1.143	0.877
T3 y	1.503	0.910
T2 x	1.268	0.876
T2 y	1.225	0.941
T1 x	1.221	0.912
T1 y	1.277	0.927
JAW x	0.581	0.828
JAW y	0.722	0.914
UL x	0.324	0.840
UL y	0.454	0.843
UL x	0.647	0.875
UL y	1.083	0.905
Average	<b>0.9544</b>	<b>0.8877</b>

Table 4.8: Per articulator RMSE and correlation performance on the MNGU0 test dataset of a 3 hidden layer ANN with 300 units per hidden layer, pretrained as a DBN. The output of the ANN is low-pass filtered using the cut-off frequencies on Table 4.6 on page 35.

The new results of our system after low-pass filtering surpass the best results of Richmond’s trajectory mixture density networks, even using a much simpler dynamical model. Best results were obtained using a 3 hidden-layer architecture with 300 units per layer with a record average RMS error of 0.9544 mm and an average correlation with the real articulatory trajectory of 0.888 on the test set of the MNGU0 dataset. A per articulator report of RMS error and correlation can be found on Table 4.8.

### 4.3 Output augmentation, multitask learning

Given that our dataset was kindly provided by Korin Richmond, whose work on trajectory mixture density networks requires articulatory data augmented with delta (velocity) and delta-delta (acceleration) features, our data also included this kind of features. We have noticed that training our system using these extra output features tends to improve the accuracy of our estimations when using a deep architecture with 3 hidden layers<sup>4</sup>, as shown in Figure 4.11 on the next page.

These results may seem paradoxical: it could be thought that adding more output features

<sup>4</sup>It also improves, sometimes, the accuracy of the 2 hidden-layer models, but not consistently. We do not know whether this improvement is not reflected on the 1 hidden layer model because more than one hidden layer is required or because more hidden units would be needed.

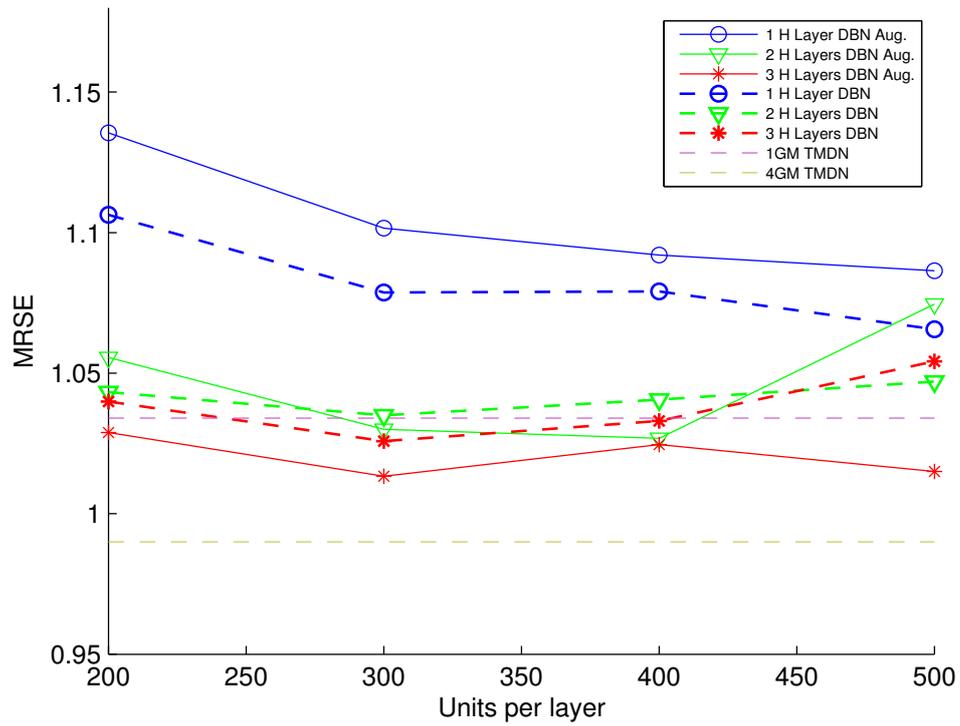


Figure 4.11: Comparison of RMSE performance on the MNGU0 test dataset of ANNs pre-trained as DBNs. Solid lines show the RMSE of ANNs trained with augmented (velocity and acceleration) output features. Solid lines show the accuracy of ANNs trained only with static output features.

	RMSE (mm)	Correlation
T3 x	1.150	0.880
T3 y	1.526	0.912
T2 x	1.268	0.881
T2 y	1.218	0.942
T1 x	1.189	0.919
T1 y	1.274	0.927
JAW x	0.580	0.829
JAW y	0.716	0.917
UL x	0.319	0.847
UL y	0.445	0.854
UL x	0.639	0.879
UL y	1.074	0.908
Average	<b>0.9501</b>	<b>0.8916</b>

Table 4.9: Per articulator RMSE and correlation performance on the MNGU0 test dataset of a 3 hidden layer ANN with 300 units per hidden layer, pretrained as a DBN and fine-tuned using augmented outputs. The output of the ANN is low-pass filtered using the cut-off frequencies on Table 4.6 on page 35.

would interfere with the learning of features useful for the outputs we are really interested in, and “compete” for the use of the internal representations. However, the beneficial effect of augmenting the output with the right kind features has been previously recognised and studied and is known as “multitask learning” [7].

Multitask learning argues that by trying to learn several related tasks at the same time, the internal representation that is learned for one task can be useful in learning another task.

We ignore what kind of internal representations do dynamic (velocity and acceleration) output features add to our network, but they appear to be useful in the light of results. We have found a clue for the kind of representation forced by augmentation of the output, when we low-pass filtered the output. As can be observed in Figure 4.12 on the following page, most of the improvement acquired by doing output augmentation is lost after low-pass filtering. This could indicate that dynamical augmentation of the output encouraged the internal representation in the hidden layers to learn continuity features [42].

Regardless, the augmented-output 3 hidden-layer architecture with 300 units per layer achieved slightly better results than the non-augmented version, with a record RMSE of 0.9501 mm and a correlation with the real articulatory trajectory of 0.892 on the test set of the MNGU0 dataset. A per articulator report of RMS error and correlation can be found on Table 4.9.

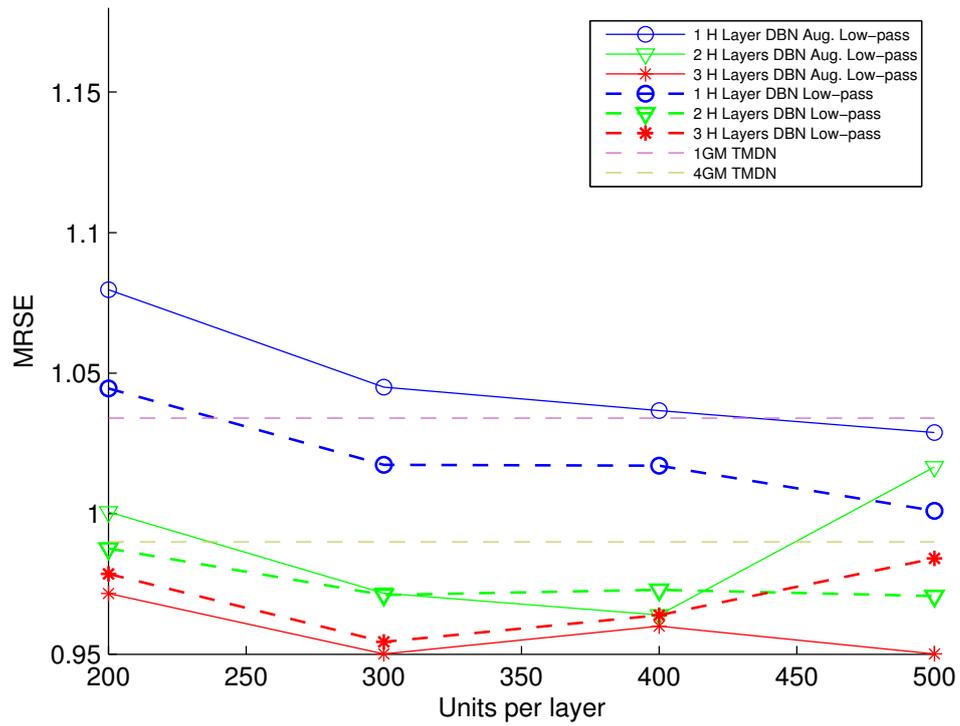


Figure 4.12: Comparison of RMSE performance on the MNGU0 test dataset of ANNs pre-trained as DBNs after low-pass filtering the output. Solid lines show the RMSE of ANNs trained with augmented (velocity and acceleration) output features. Solid lines show the accuracy of ANNs trained only with static output features.

Unfortunately, due to the heavy computational burden of training these models, we have not been able yet to repeat the experiments with augmented outputs a sufficient number of times to discard the possibility of the improvement seen being just a coincidence.



## Chapter 5

# Conclusion

### 5.1 Contributions

In this work we have implemented what is, to the best of our knowledge, the first deep architecture for articulatory inversion. We have shown that this kind of architectures are capable of obtaining accurate estimations of the articulatory trajectories. Best results were obtained using 3 hidden layers of 300 units each, with an RMSE of 0.95 mm on the test set of the MNGU0 dataset. A significant error reduction compared to the previous best results published on the same dataset of 0.99 mm using trajectory mixture density networks.

In our work, we show that adding hidden layers (up to three) to the architecture, improves the accuracy. We also show, this is a result of a higher expressive capability of a deep architecture [4], and not only a result of adding more parameters to the model, since a shallow model with the same or more parameters was unable to equal the accuracy obtained by the 3 hidden layers model.

We also show the advantage of doing unsupervised pretraining, where a deep belief network is trained before being transformed into an artificial neural network. In all cases analysed this had a positive effect on the results.

### 5.2 Limitations

There are two main limitations in our work. The first one is procedural: in order to claim that our system is better than previous published work, we would need to repeat our experiments a number of times, obtain averages of the accuracies and calculate error intervals. However, as explained in Appendix A, training these models has a high computational cost and no time for it was available. Nevertheless, we are confident our results will hold as

the improvement over previous methods are quite significant in magnitude and are present across a variety of number of hidden layers and units per layer.

The second main limitation relates to our methodology. Even though low-pass filtering improves our results considerably, it would be desirable to implement a more advanced trajectory method as it is done in the most recent publications by Richmond [45] or Renals [56]. Using the maximum likelihood parameter generation algorithm requires a probability distribution of the position, velocity and acceleration of the articulators. However, our present system is only capable of inferring point estimates of those features.

### 5.3 Future work

In order to be able to use the maximum likelihood parameter generation algorithm, we intend to adapt our present system to act as a “deep” mixture density network. To do this we will have to modify our system to have as output features the mean, covariance matrix and mixing factors of a Gaussian mixture model. These changes only affect the backpropagation phase of the training and not the unsupervised pretraining stage. Besides, having a Gaussian mixture as the output of our system will also allow us to explicitly tackle the non-uniqueness of the articulatory inversion problem, leaving for the MLPG algorithm to decide the most likely trajectory through that multimodal probability estimation.

Another research line worth exploring would include doing articulatory inversion from an acoustic speech representation less processed than line spectral frequencies (LSF). Although LSF appeared the best acoustic encoding for articulatory inversion in a previous comparative study by Qin and Carreira-Perpinan [38], those studies did not include the use of deep architectures. Given that deep architectures for phone recognition obtain better results using simple encodings like filterbank coefficients, we hypothesise those improvements could also be translated to the articulatory inversion domain.

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## Appendix A

### Computational setup

Comparing the performance of our GPU-based system with an initial CPU implementation we obtained a 20-fold reduction of training times when using nVidia GTX480 GPU compared with single core of an Intel Core i7 930 CPU (5-fold when using 6 CPU cores).

However, the use of a GPU comes with some limitations, namely our system had 1.5 GB of GPU memory which limited the number of units per layer to about 500 if we wanted to keep the internal representations of the whole MNGU0 training dataset in the GPU's memory. A way to avoid this problem is to feedforward through previous layers the data just when it is needed. Unfortunately, that solution takes away a good portion of the GPU speed-up.

Even taking advantage of GP-GPU processing, training a restricted Boltzmann machine is a slow process. Training an RBM with 300 units in each layer takes about 30 seconds per epoch, an RBM with 500 units per layer about 60s per epoch. Given that a typical training experiment requires about 200 epochs, it amounts to 1.5 to 3 hours. The training times are multiplied by the fact that an RBM has to be trained for each layer of the deep belief network, and the many experiments required to find appropriate values for the training configuration.

The backpropagation fine-tuning process was also implemented using GP-GPU processing. It was found to take 1 to 3 hours depending on the number of layers and units per layer, obtaining a 2.5 fold reduction of training times compared to using 6 CPU cores. Even though faster algorithms could have been implemented for the fine-tuning phase, for example scaled conjugate gradients optimization, we considered the simple backpropagation algorithm satisfactory enough, given that most of the training time is spent, anyway, training the restricted Boltzmann machines.